

1 $\forall x (P(x) \Rightarrow (\exists y i(y, x)))$ mai 2017

$$\boxed{\neg P(x) \vee i(y, x)}$$

2 $\forall x \forall y [(P(x) \wedge i(y, x)) \Rightarrow m(y)]$

$$\boxed{\neg P(x) \vee \neg i(y, x) \vee m(y)}$$

3 $\exists x (P(x) \wedge (\forall y [m(y) \Rightarrow a(x, y)]))$

$$P(c) \wedge (\neg m(y) \vee a(c, y))$$

$$\begin{array}{l} \exists_a \boxed{P(c)} \\ \exists_b \boxed{\neg m(y) \vee a(c, y)} \end{array}$$

4 $\forall x [(P(x) \wedge \neg r(x)) \Rightarrow \neg (\forall y (m(y) \Rightarrow a(x, y)))]$

$$\forall x \exists y (\neg P(x) \vee r(x) \vee [m(y) \wedge \neg a(x, y)])$$

$$4_a \boxed{\neg P(x) \vee r(x) \vee m(y(x))}$$

$$4_b \boxed{\neg P(x) \vee r(x) \vee \neg a(x, y(x))}$$

5 $\exists x (P(x) \wedge r(x) \wedge [\exists y (i(y, x) \wedge a(x, y))])$

$$\neg \exists x \forall y \neg P(x) \vee \neg r(x) \vee \neg i(y, x) \vee \neg a(x, y)$$

$$5 \boxed{\neg P(x) \vee \neg r(x) \vee \neg i(y, x) \vee \neg a(x, y)}$$

$$1 \quad \neg p(x) \vee i(f(x), x)$$

$$2 \quad \neg p(x) \vee \neg i(y, x) \vee m(y)$$

$$3a \quad p(c)$$

$$3b \quad \neg m(y) \vee a(c, y)$$

$$4a \quad \neg p(x) \vee r(x) \vee m(g(x))$$

$$4b \quad \neg p(x) \vee r(x) \vee \neg a(x, g(x))$$

$$7C:5 \quad \neg p(x) \vee \neg r(x) \vee \neg i(y, x) \vee \neg a(x, y)$$

3a $p(c)$ unifier $x=c$ puis compose

$$1 \vdash i(f(c), c) \quad A$$

$$2 \quad \neg i(y, c) \vee m(y) \quad B$$

$$4a \quad r(c) \vee m(g(c)) \quad C$$

$$4b \quad r(c) \vee \neg a(c, g(c)) \quad D$$

$$5 \quad \neg r(c) \vee \neg i(y, c) \vee \neg a(c, y) \quad E$$

$$3b \quad y \in g(c) / \neg m(y) \vee a(c, y) \vdash \neg m(g(c)) \vee a(c, g(c))$$

$$3a \vee C \quad r(c) \vee m(g(c)) \vdash r(c) \vee a(c, g(c)) \quad F$$

$$FD \quad r(c) \vee \neg a(c, g(c)) \vdash r(c) \quad G$$

E $\neg(c)$
 G $\neg\neg(c) \vee \neg i(y, c) \vee \neg a(c, y) \vdash \neg i(y, c) \vee \neg a(c, y)$ ~~$\vdash \neg a(c, y)$~~

H $y \in f(c) \quad i(f(c), c)$
 B $\neg i(f(c), c) \vee \neg a(c, f(c)) \vdash \neg a(c, f(c))$ I

I 3b $\neg a(c, f(c))$
 $\neg m(y) \vee a(c, y)$
 $y \in f(c) \vdash \neg m(f(c))$ J

A, B $i(f(c), c)$
 $\neg i(y, c) \vee m(y)$
 $y \in f(c) \vdash m(f(c))$ K

J K $\vdash \perp$